

Measurement of Collins Asymmetries in e^+e^- Annihilation at Belle

AGS&RHIC Users' Meeting

June 19th , Brookhaven National Laboratory

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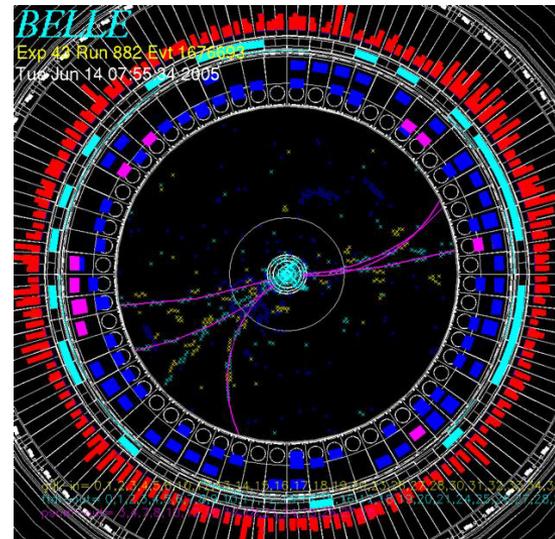
Illinois

BNL and RBRC

Illinois and RBRC

RBRC

for the Belle Collaboration





----- Outline -----

○ Motivation

- Collins FF for global QCD analysis of single transverse asymmetries in pp and SIDIS

○ Collins Asymmetries from e^+e^-

- LEP first work on Delphi data in the 90s:
Efremov, Smirnova, Tkatchev and Bonivento, Matteuzzi, Kotzinian
- Experimental technique
- Results





Why is the Collins Fragmentation Function Interesting?

- o Very basic QCD process: Fundamental test case for any approach to solve QCD at soft scales.
- o Tests of universality and factorization between $e+e^-$, DIS and p-p collisions
- o Symmetry properties
- o Evolution is fundamental QCD prediction
- o Connection between microscopic and macroscopic observables:

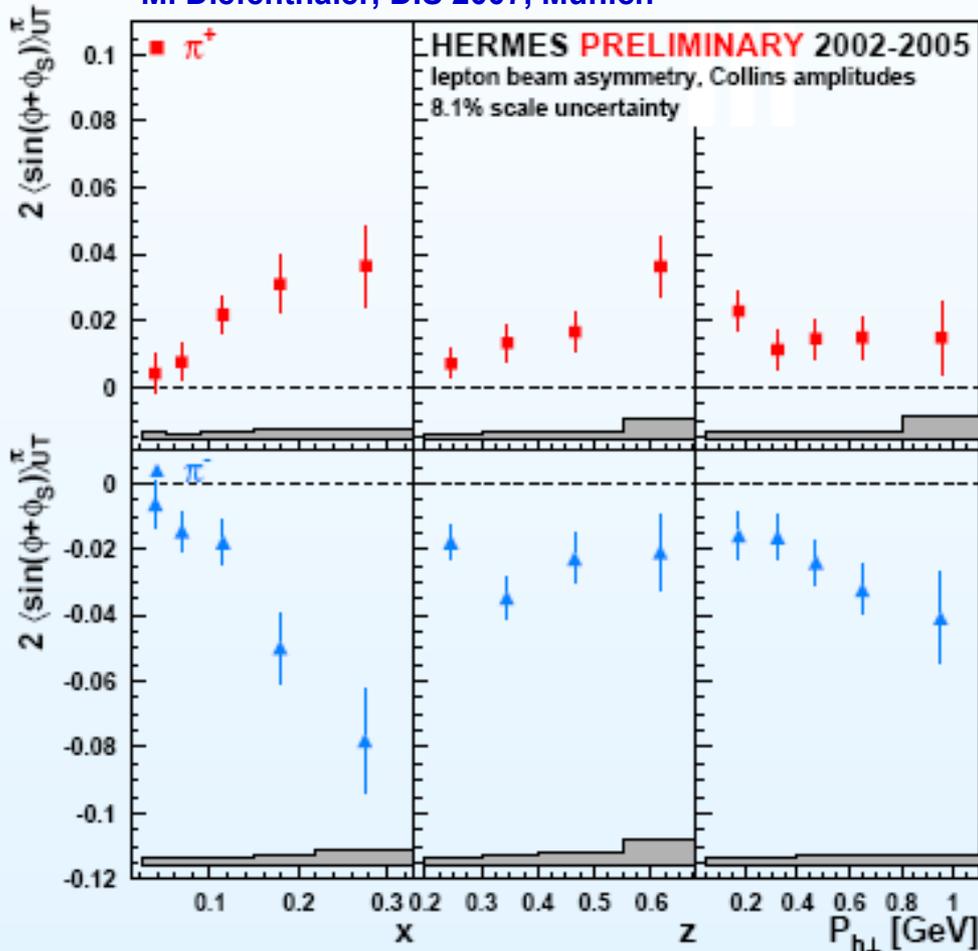
→ Probe/analyzer for transverse quark spin
critical input for transverse proton spin program
at DESY, CERN, JLab and RHIC





Motivation Transversity Quark Distributions from Collins- and Interference-Fragmentation

New HERMES results for Collins Asymmetries
M. Diefenthaler, DIS 2007, Munich



Collins- and IFF- asymmetries in SIDIS and pp are of the form

$$\sim \text{Transversity}(x) \times \text{CFF}(z)$$

$$\sim \text{Transversity}(x) \times \text{IFF}(z)$$

Collins- and IFF- asymmetries in e^+e^- are of the form

$$\sim \text{CFF}(z_1) \times \text{CFF}(z_2)$$

$$\sim \text{IFF}(z_1) \times \text{IFF}(z_2)$$

→ global QCD analysis





Global Analysis: Extract Transversity Distributions

SIDIS \Rightarrow

transversity \times Collins

transversity \times IFF

HERMES, COMPASS,

JLAB, EIC

Factorization

+

Universality ?!

$e^+e^- \Rightarrow$ Collins \times Collins

Interference FF

\times Interference FF

Belle

Transversity
Tensor Charge

RHIC / GSI

pp \Rightarrow

A_N for inclusive hadrons, Jets

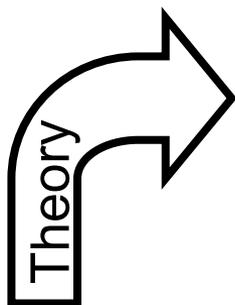
A_T in Jets: transversity \times Collins

transversity \times IFF

GSI

A_{TT} Drell Yan:

transversity \times transversity



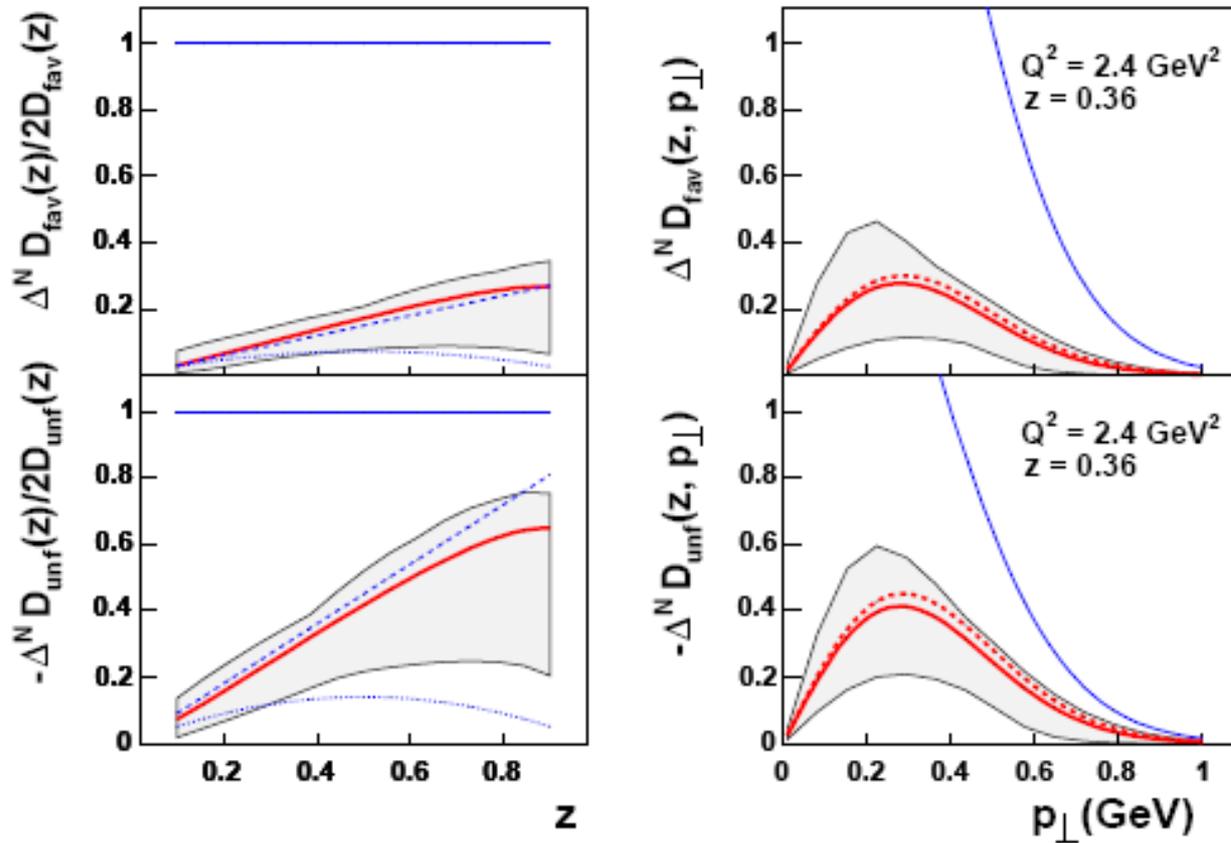
Lattice QCD: Tensor Charge





First QCD Analysis of SIDIS + e^+e^- !

Anselmino, Boglione, D'Alesio,
Kotzinian, Murgia, Prokudin, Turk
Phys. Rev. D75:05032,2007



Fit includes:

HERMES SIDIS
+ COMPASS SIDIS
+ Belle e^+e^-

→ transversity dist.
+ Collins FF

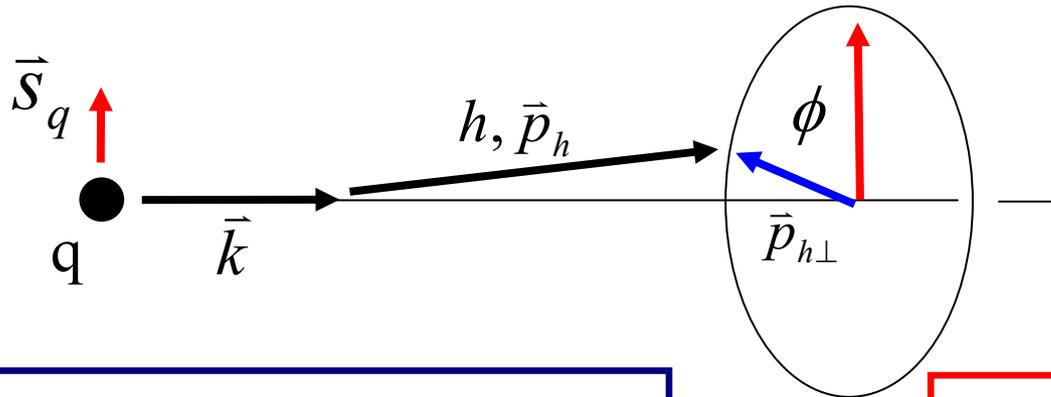


Measurement of Collins Asymmetries In e^+e^- at KEK B with the Belle

Phys.Rev.Lett.96:232002,2006
and update at Spin 2006 in Kyoto

Collins Effect in Quark Fragmentation

J.C. Collins, Nucl. Phys. B396, 161(1993)



- \vec{k} : quark momentum
- \vec{s}_q : quark spin
- \vec{p}_h : hadron momentum
- $\vec{p}_{h\perp}$: transverse hadron momentum
- $z_h = E_h/E_q$
 $= 2 E_h/\sqrt{s}$: relative hadron momentum

Collins Effect:
 Fragmentation of a transversely polarized quark q into spin-less hadron h carries an azimuthal dependence:
 $\propto (\vec{k} \times \vec{p}_{h\perp}) \cdot \vec{s}_q$
 $\propto \sin \phi$





General Form of Fragmentation Functions

Number density for finding
hadron h from a transversely
polarized quark, q :

$$D_{q\uparrow}^h(z, \vec{p}_{h\perp}) = \underbrace{D_1^{q,h}(z)}_{\text{unpolarized FF}} + \underbrace{H_1^{\perp q,h}(z, p_{h\perp}^2)}_{\text{Collins FF}} \frac{(\hat{k} \times \vec{p}_{h\perp}) \cdot \vec{s}_q}{zM_h}$$



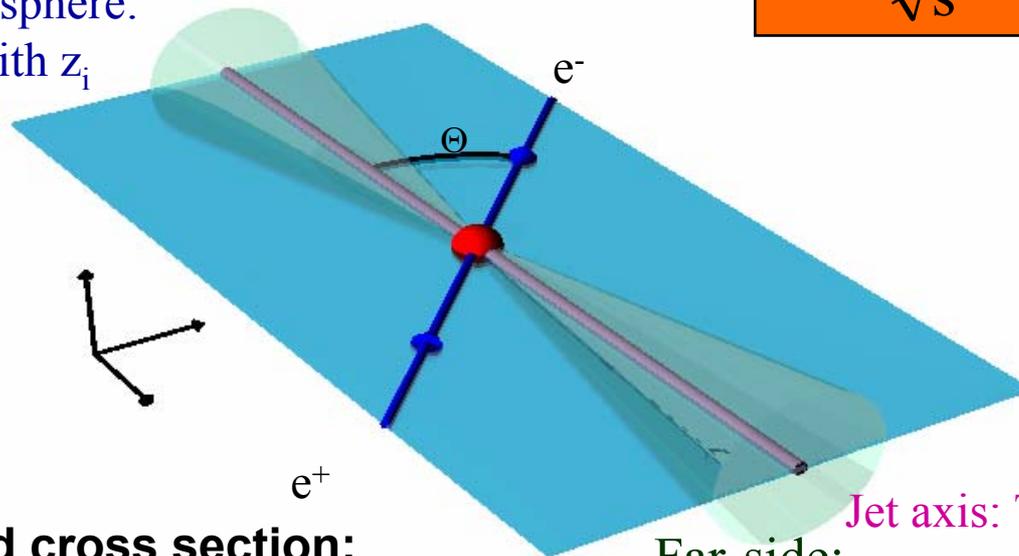
Event Structure at Belle

e^+e^- CMS frame:

$$z = \frac{2E_h}{\sqrt{s}}, \quad \sqrt{s} = 10.52 \text{ GeV}$$

Near-side Hemisphere:

$h_i, i=1, N_n$ with z_i



$$\langle N_{h^{+,-}} \rangle = 6.4$$

Spin averaged cross section:

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2} = \frac{3\alpha^2}{Q^2} A(y) \sum_{a, \bar{a}} e_a^2 D_1(z_1) \bar{D}_1(z_2)$$

$$A(y) = \left(\frac{1}{2} - y + y^2 \right)^{(cm)} = \frac{1}{4} (1 + \cos^2 \Theta)$$

Far-side:

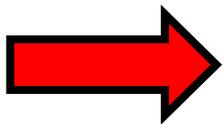
$h_j, j=1, N_f$ with z_j

Jet axis: Thrust



Collins FF in e^+e^- : Need Correlation between Hemispheres !

- Quark spin direction unknown: measurement of Collins function in one hemisphere is not possible $\sin \varphi$ modulation will average out.
- Correlation between two hemispheres with $\sin \varphi_i$ Collins single spin asymmetries results in $\cos(\varphi_1 + \varphi_2)$ modulation of the observed di-hadron yield.

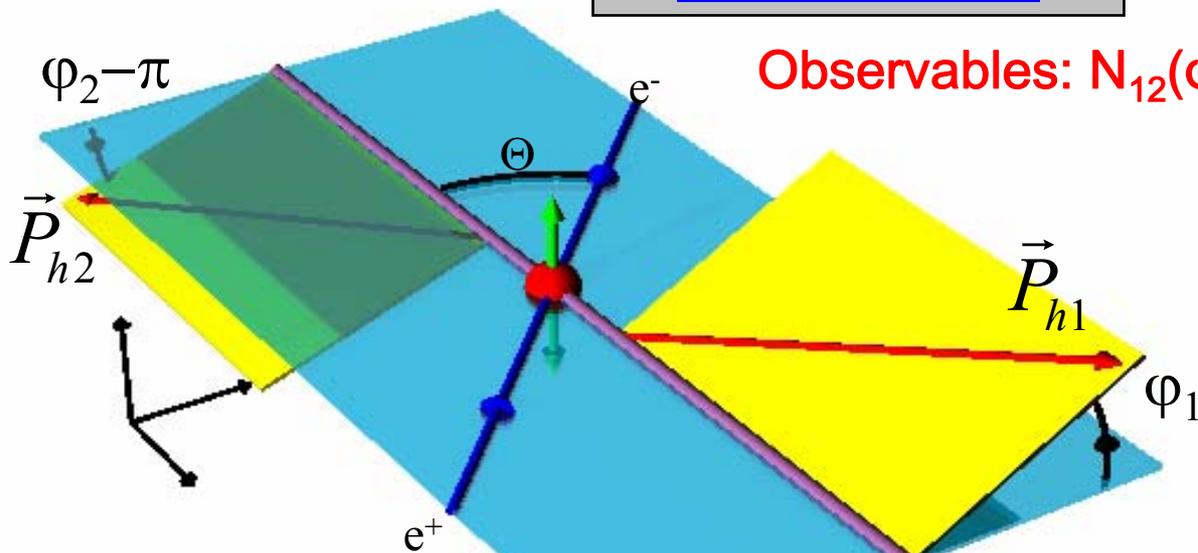


Measurement of azimuthal correlations for pion pairs around the jet axis in two-jet events!

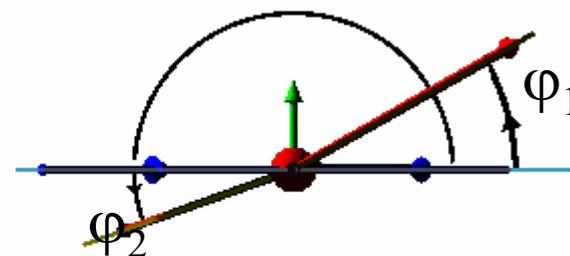


Collins Fragmentation: Angles and Cross Section $\cos(\phi_1 + \phi_2)$ Method

e^+e^- CMS frame:



Observables: $N_{12}(\phi_1 + \phi_2)$, $A_{12}(z_1, z_2)$



2-hadron inclusive transverse momentum dependent cross section:

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d^2q_T} = \dots B(y) \cos(\phi_1 + \phi_2) H_1^{\perp[1]}(z_1) \bar{H}_1^{\perp[1]}(z_2)$$

$$B(y) = y(1-y) \stackrel{\text{cm}}{=} \frac{1}{4} \sin^2 \Theta$$

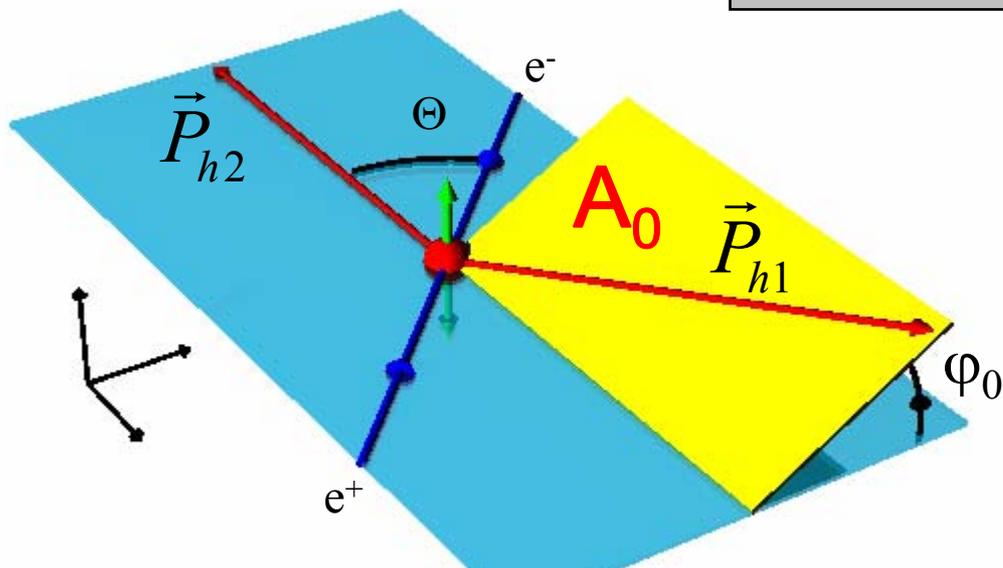
Net anti-alignment of transverse quark spins



Collins Fragmentation: Angles and Cross Section $\cos(2\phi_0)$ Method

Observables: $N_0(\phi_0)$, $A_{12}(z_1, z_2)$

e^+e^- CMS frame:



- Independent of thrust-axis
- Convolution integral I over transverse momenta involved

[Boer, Jakob, Mulders:
NPB504(1997)345]

2-hadron inclusive transverse momentum dependent cross section:

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d^2q_T} = \dots B(y) \cos(2\phi_0) \left[\left(\hat{z} \cdot \hat{h} \cdot \hat{h} \cdot p_T - k_T \cdot p_T \right) \frac{H_1^+ \bar{H}_1^+}{M_1 M_2} \right]$$

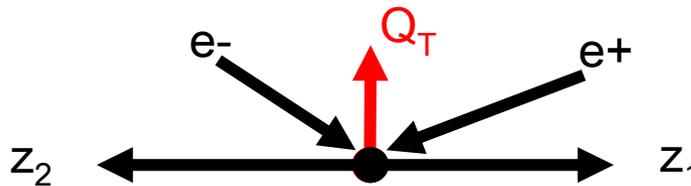
$$B(y) = y(1-y) \stackrel{\text{cm}}{=} \frac{1}{4} \sin^2 \Theta$$

Net anti-alignment of
transverse quark spins



Gluon Emission

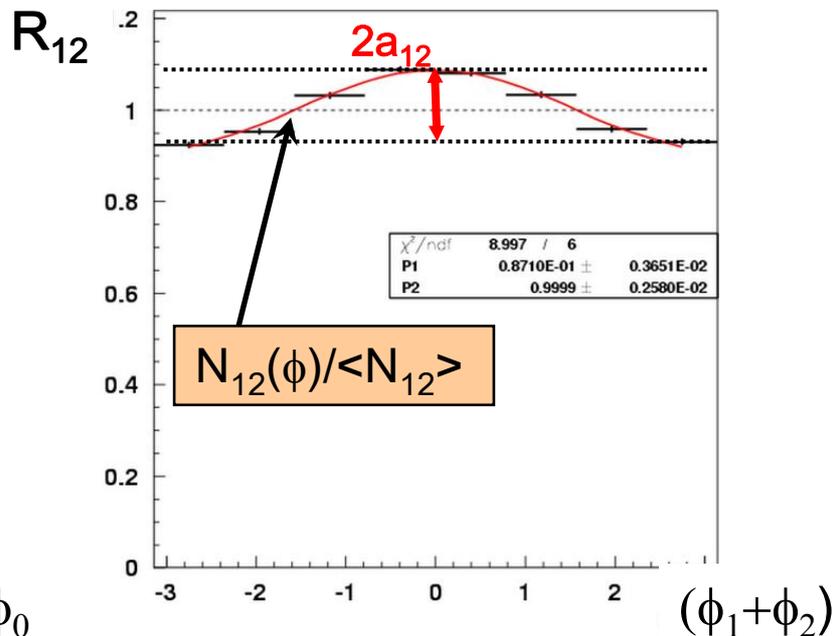
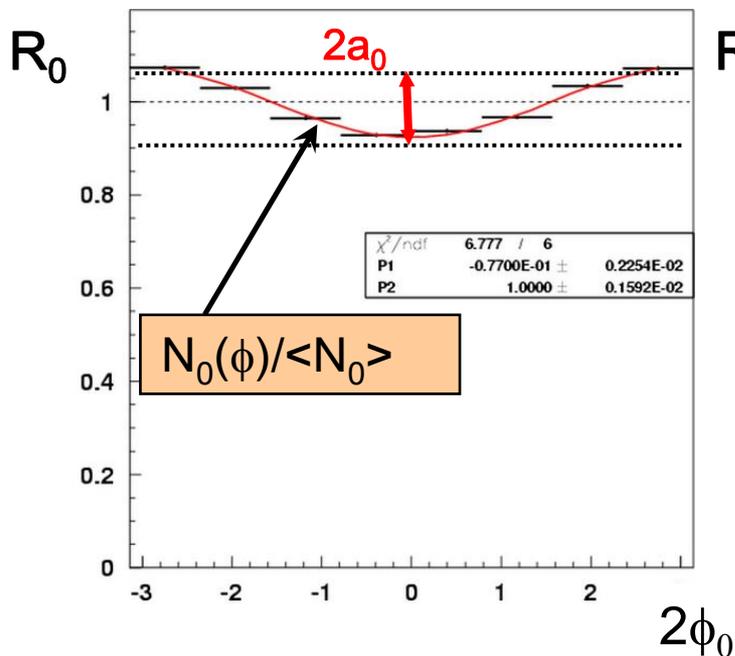
$$\frac{dN}{d\Omega dz_1 dz_2 dq_T} \propto \sum \left[\frac{q_T^2}{Q^2 + Q_T^2} \sin^2 \theta \cos(2\phi_0) D_1(z_1) \bar{D}_1(z_2) \right]$$



Frame:

$$\vec{p}_1 = -\vec{p}_2$$

Examples of Fits to Azimuthal Asymmetries



$$R_0 = \frac{N_0(\phi_0)}{\langle N_0 \rangle} \propto \frac{aD_1\bar{D}_1 + \cos(\phi_0)[bH_1\bar{H}_1 + cD_1\bar{D}_1]}{aD_1\bar{D}_1} = b_0 + a_0 \cos(\phi_0)$$

D_1 : spin averaged fragmentation function,

H_1 : Collins fragmentation function



Method to eliminate gluon contributions: Double ratios for unlike- and like sign pions

Form double ratios for unlike and like-sign pion pairs:

$$R = \frac{R_{12}^{UnLike-sign}}{R_{12}^{Like-sign}} = \frac{N_{12}^{UL}(\phi_1 + \phi_2)}{\langle N_{12} \rangle} \bigg/ \frac{N_{12}^L(\phi_1 + \phi_2)}{\langle N_{12} \rangle}$$
$$\approx 1 + \frac{1}{4} \cos(\phi_1 + \phi_2) A_{12}^{UL/L}(z_1, z_2)$$

(I) radiative effects are charge independent and cancel.

(II) R^{UL} and R^L depend on H^{fav} and H^{dis} differently.

→ A_{12} retains sensitivity for the Collins effect!

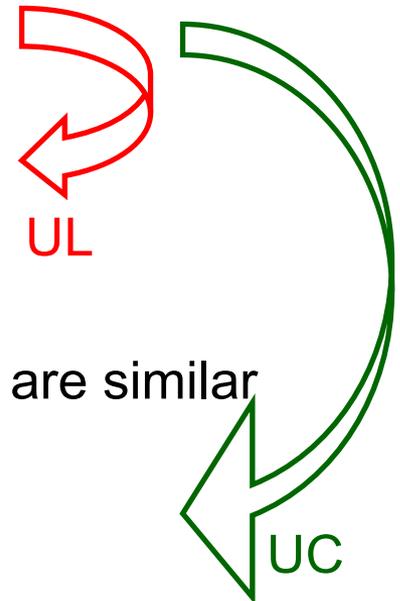
$$A_{12}^{UL/L}(z_1, z_2) = \frac{\sin^2 \theta}{1 + \cos^2 \theta} \left(\frac{H_1^{fav} H_2^{fav} + H_1^{dis} H_2^{dis}}{D_1^{fav} D_2^{fav} + D_1^{dis} D_2^{dis}} - \frac{H_1^{fav} H_2^{dis} + H_1^{dis} H_2^{fav}}{D_1^{fav} D_2^{dis} + D_1^{dis} D_2^{fav}} \right)$$



Two Double Ratios

Double ratios unlike/like-sign not very sensitive in separating favored and disfavored Collins functions → look at unlike-sign/charge-sum

- Unlike-sign pion pairs (**U**):
(favored x favored + unfavored x unfavored)
- Like-sign pion pairs (**L**):
(favored x unfavored + unfavored x favored)
- $\pi^\pm\pi^0$ pairs
(favored + unfavored) x (favored + unfavored)
- A. Efremov et al. ([hep-ph/0603054]): charged $\pi\pi$ pairs are similar (and easier to handle) (**C**):
(favored + unfavored) x (favored + unfavored)



Observables:

$$A_{12}(\text{UL}), A_{12}(\text{UC})$$

$$A_0(\text{UL}), A_0(\text{UC})$$

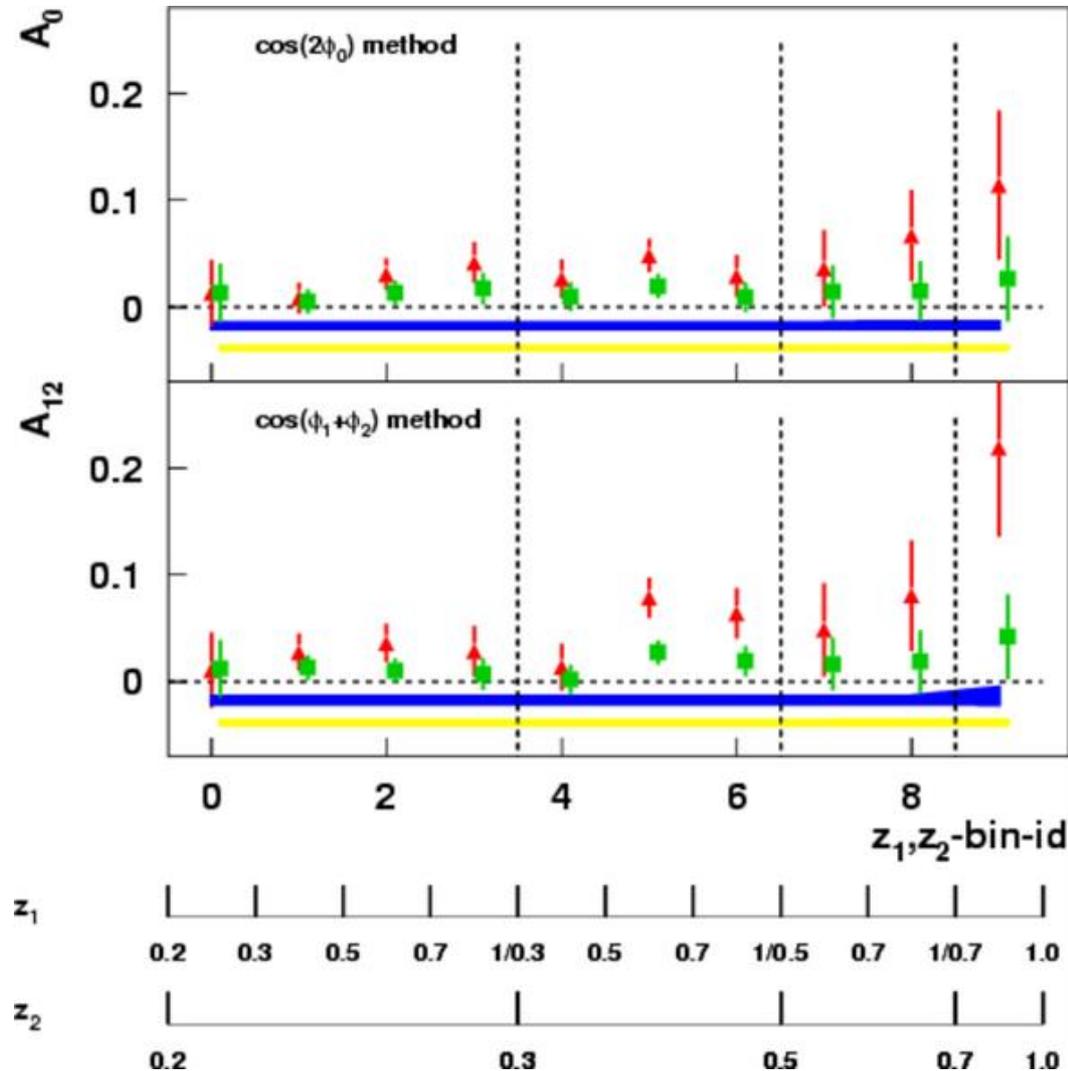
published and input to fit by Anselmino et al.



Final Charm Corrected Results for $e^+ e^- \rightarrow \pi \pi X$ (29fb⁻¹, off-resonance Data)

Phys.Rev.Lett.96:232002,2006

- Significant non-zero asymmetries
- Rising behavior vs. z
- **UL/C** asymmetries about 40-50% of **UL/L** asymmetries
- First direct measurements of the Collins function
- UL/L data published



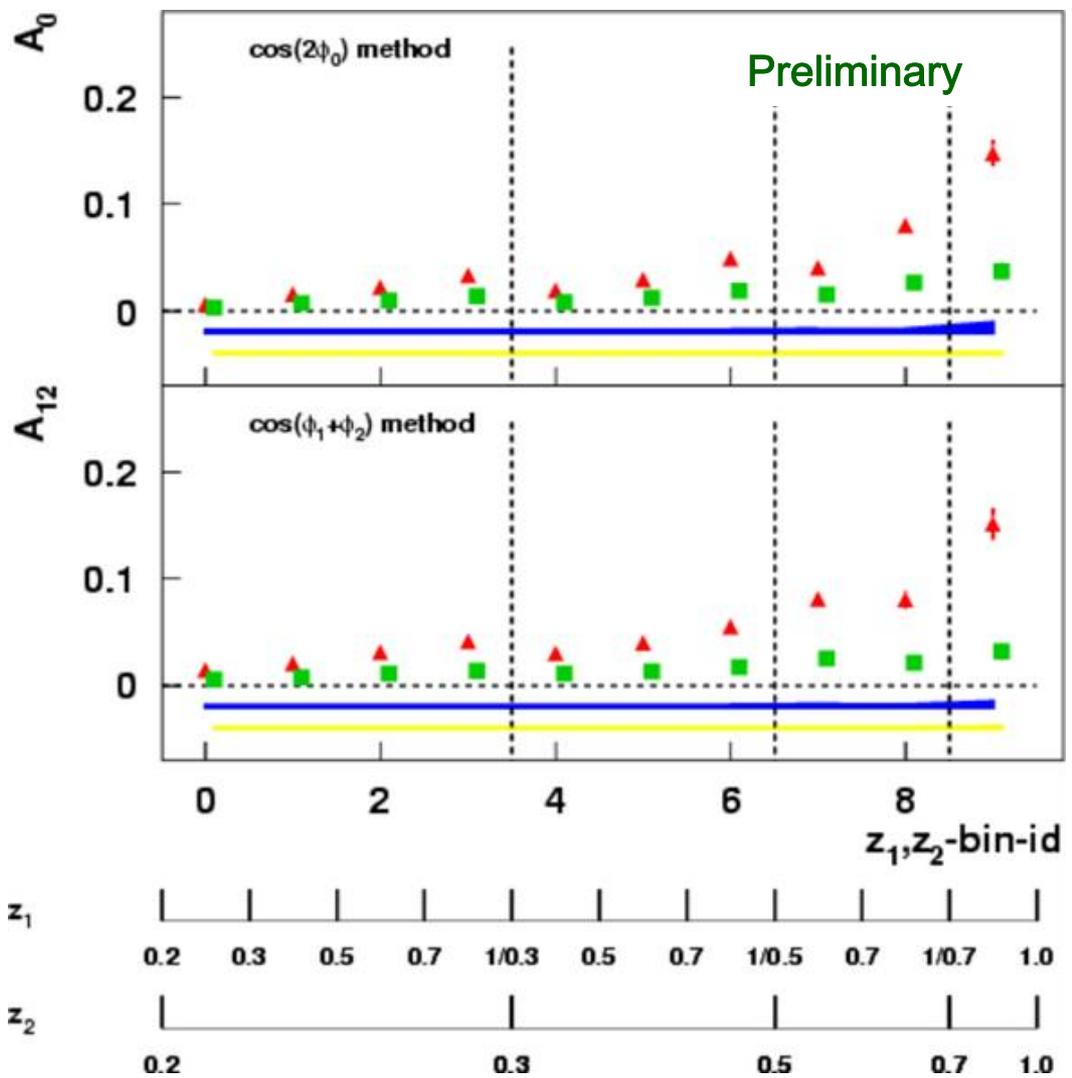
$A_0(\text{UL/L})$	$(3.06 \pm 0.57 \pm 0.55)\%$
$A_{12}(\text{UL/L})$	$(4.26 \pm 0.68 \pm 0.68)\%$
$A_0(\text{UL/C})$	$(1.27 \pm 0.49 \pm 0.35)\%$
$A_{12}(\text{UL/C})$	$(1.75 \pm 0.59 \pm 0.41)\%$





Preliminary Charm Corrected Results for $e^+ e^- \rightarrow \pi \pi X$ (547 fb^{-1} , on-resonance)

- Significance largely increased
- Behavior unchanged
- Reduced systematics
- Precise measurements of the Collins function



Integrated results:

$A_0(\text{UL/L})$	$(2.67 \pm 0.10 \pm 0.26)\%$
$A_{12}(\text{UL/L})$	$(3.55 \pm 0.08 \pm 0.15)\%$
$A_0(\text{UL/C})$	$(1.11 \pm 0.11 \pm 0.22)\%$
$A_{12}(\text{UL/C})$	$(1.46 \pm 0.09 \pm 0.13)\%$





Summary

- Observation of large azimuthal asymmetries in light quark fragmentation. Updated statistics:
 $\int L dt = 29 \text{ fb}^{-1} \rightarrow 547 \text{ fb}^{-1}$
- Double ratios reliably cancel contributions from detector acceptance and gluon radiation.
- Important input for the transverse spin physics programs at RHIC, HERMES, COMPASS and JLab.
- Fundamental test case for QCD at soft scales!

&

Outlook

- Future spin dependent FFs:
 - update Collins FF
 - measure p_T dependence
 - interference fragmentation
 - Collins FF for VMs
 - Lambdas
- Precision measurement of spin averaged fragmentation functions as input to RHIC program with inclusive hadrons and future precision measurements in SIDIS.

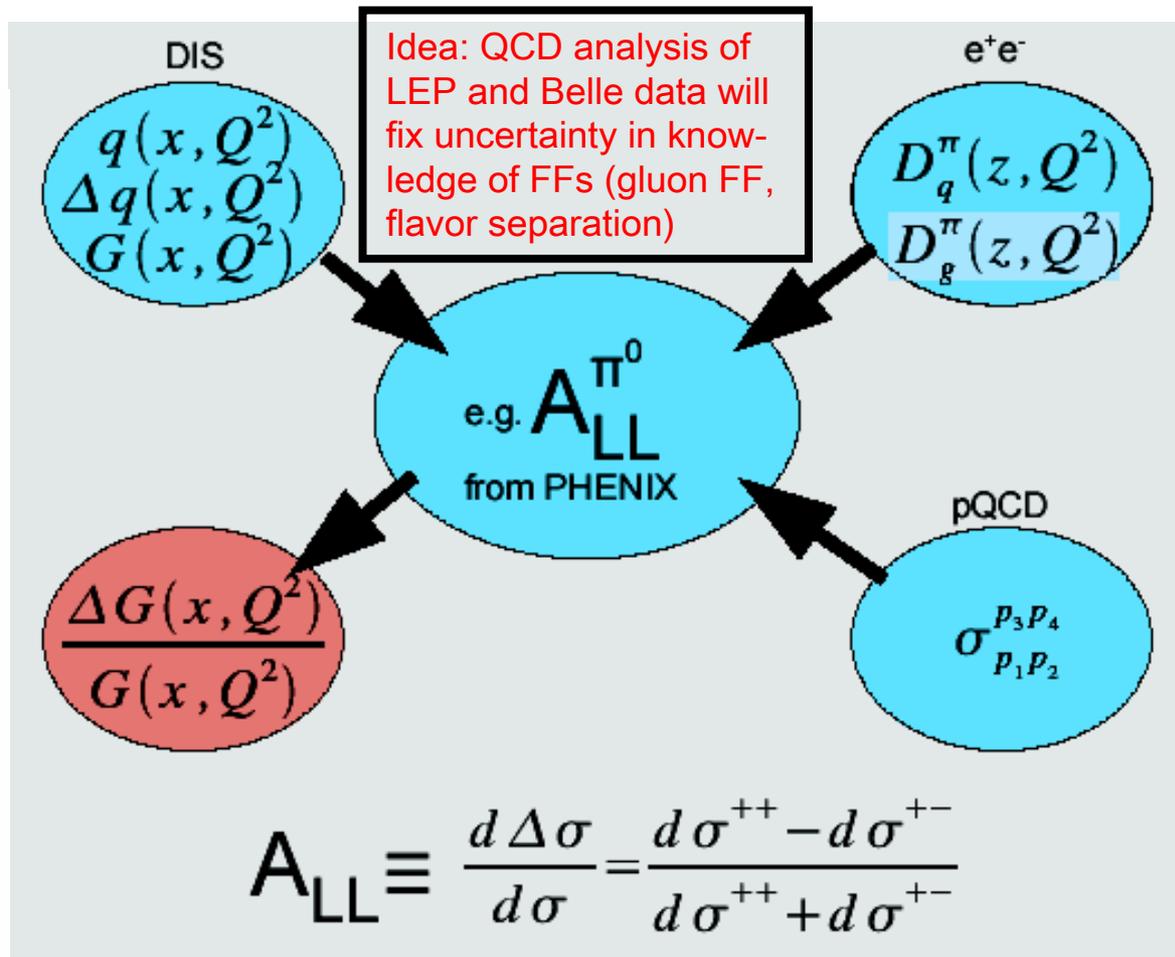
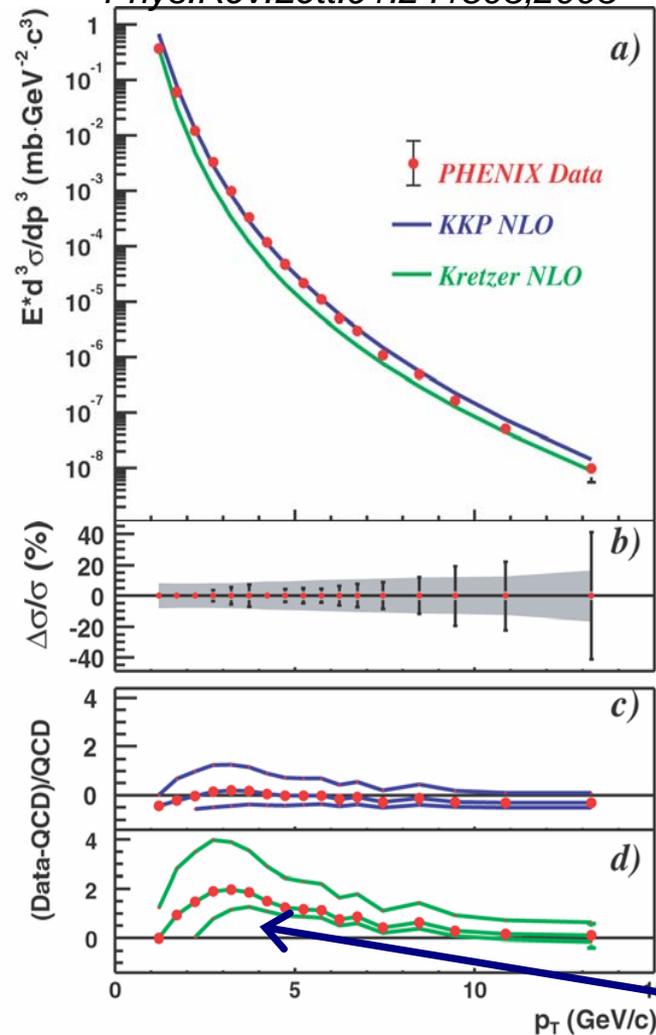




Motivation ΔG from QCD Analysis of A_{LL} for inclusive hadrons: $\pi^{0,+,-}, \eta, K^{+,-}$

PHENIX π^0 cross section at $|\eta| < 0.35$

Phys.Rev.Lett.91:241803,2003



Deviation connected to uncertainties in FFs \rightarrow gluon FF!

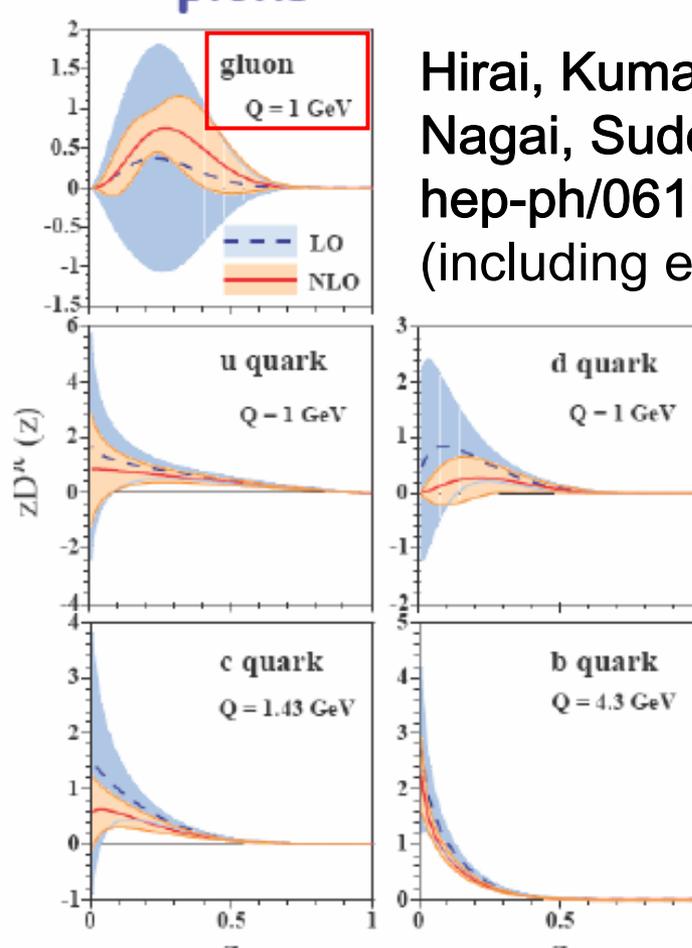
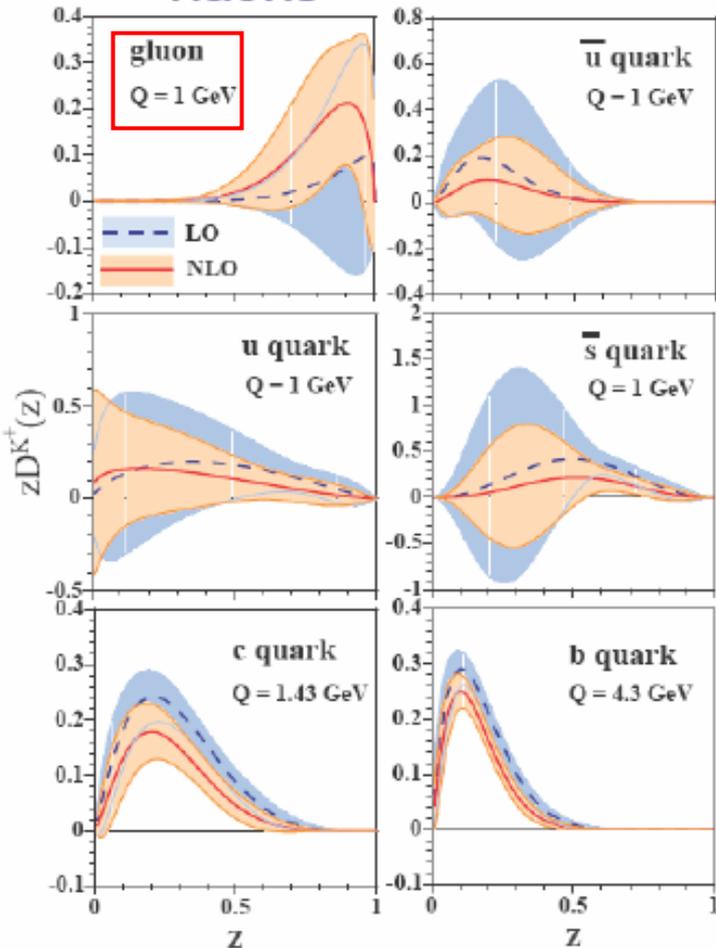




What is Known Experimentally in e^+e^- ?

kaons

pions



Hirai, Kumano,
Nagai, Sudo
hep-ph/0612009
(including errors!)

Earlier work:

Kretzer

Binnewies, Potter, Albino
Kniehl, Kramer, Potter
Albino, Kniehl, Kramer

Most recent work:

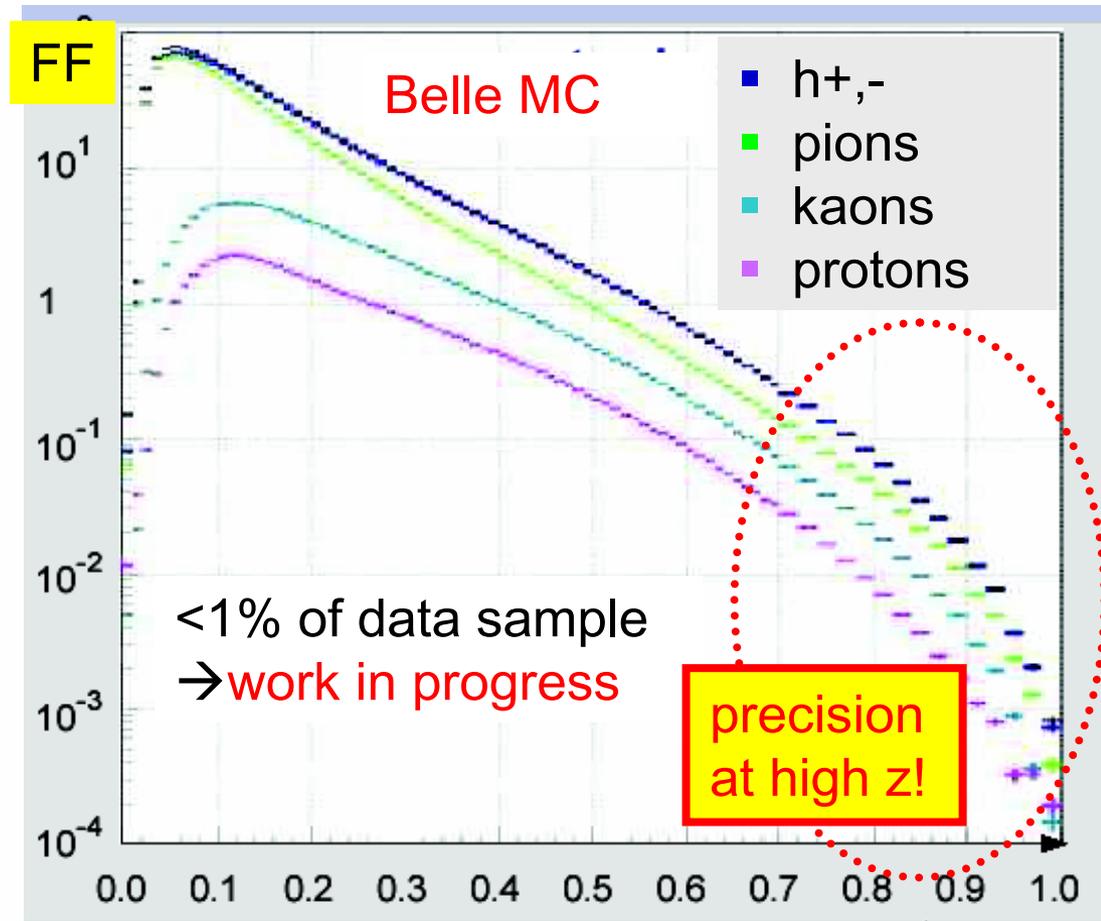
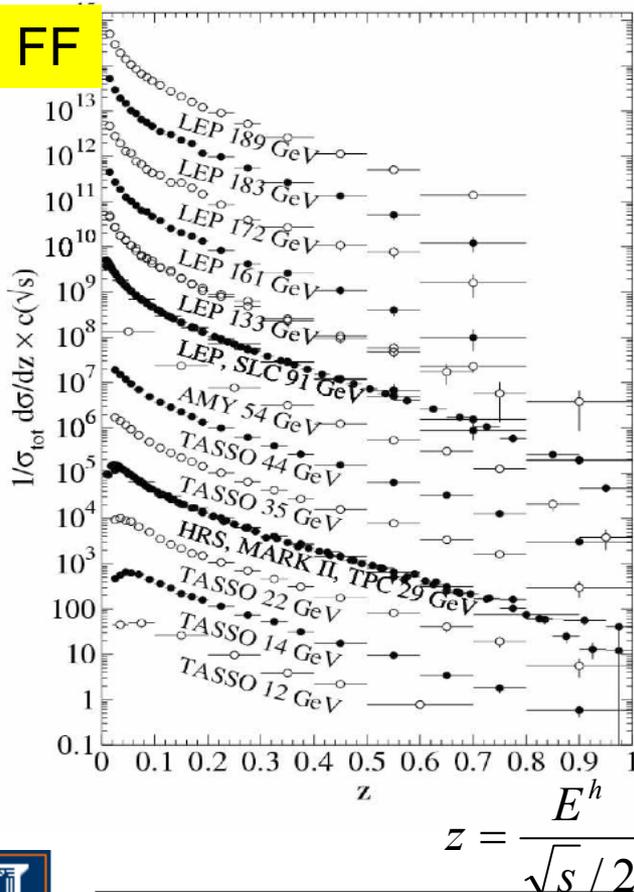
De Florian, Sassot,
Stratmann



Input also for precision measurements of quark helicity distributions in SIDIS, in particular at a possible future electron-polarized proton collider.

Impact on the Knowledge of FFs

Belle: Charged $h^{+/-}$, pions, kaons, protons



$z = \frac{E^h}{\sqrt{s}/2}$



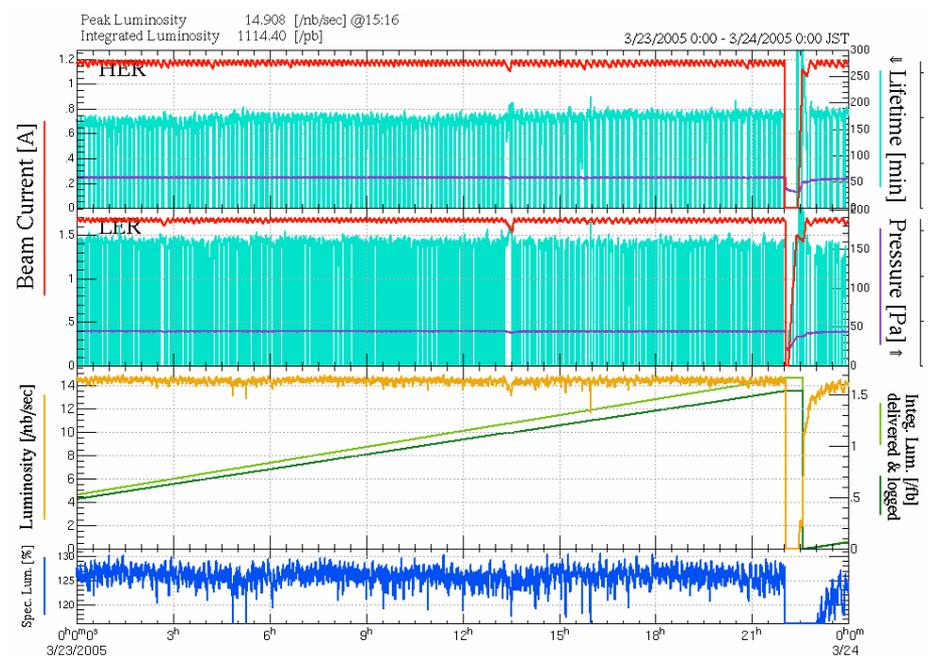
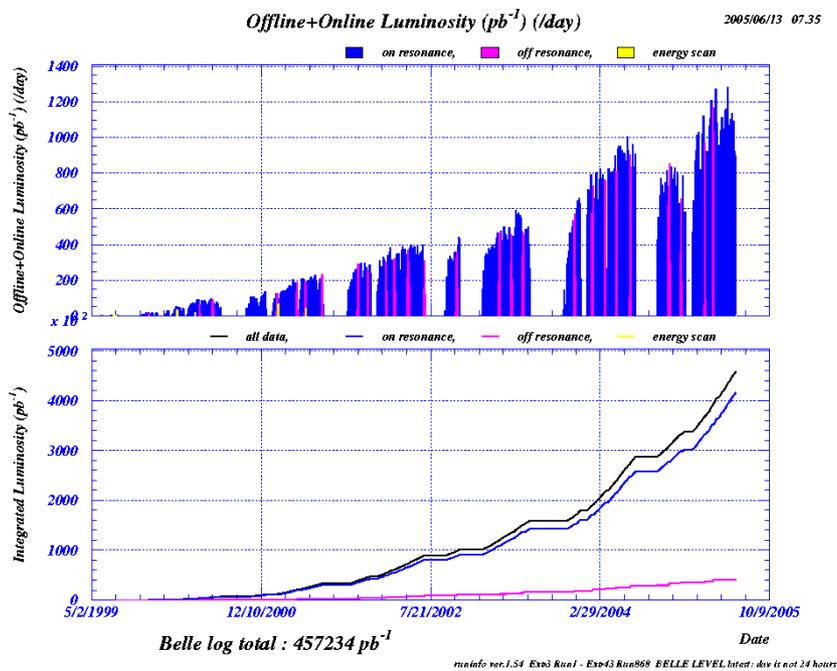


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critical input for transverse proton spin program
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KEKB: $L > 1.6 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$!!

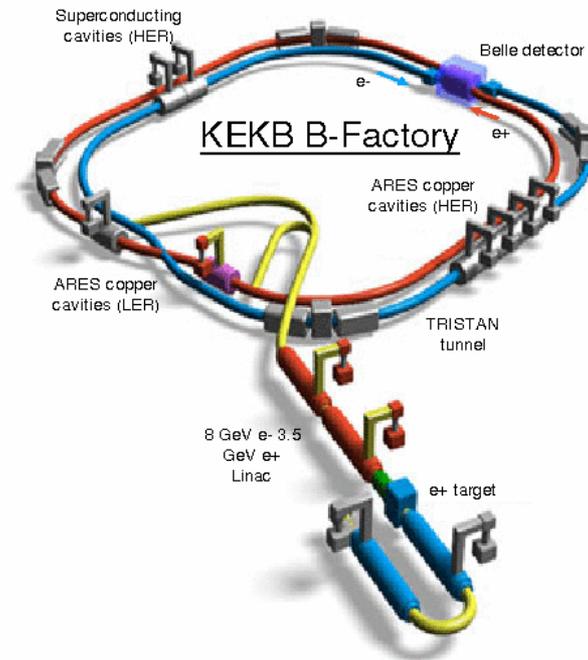
→ 1.5×10^9 hadronic events in analysis

- KEBB

- Asymmetric collider
- $8\text{GeV } e^- + 3.5\text{GeV } e^+$
- $\sqrt{s} = 10.58\text{GeV}$ ($Y(4S)$)
 $e^+e^- \rightarrow Y(4S) \rightarrow B \bar{B}$
- Off-resonance: 10.52 GeV
 $e^+e^- \rightarrow q \bar{q}$ (u,d,s,c)
- **Integrated Luminosity: $> 600 \text{ fb}^{-1}$**
 $> 60\text{fb}^{-1} \Rightarrow$ off-resonance

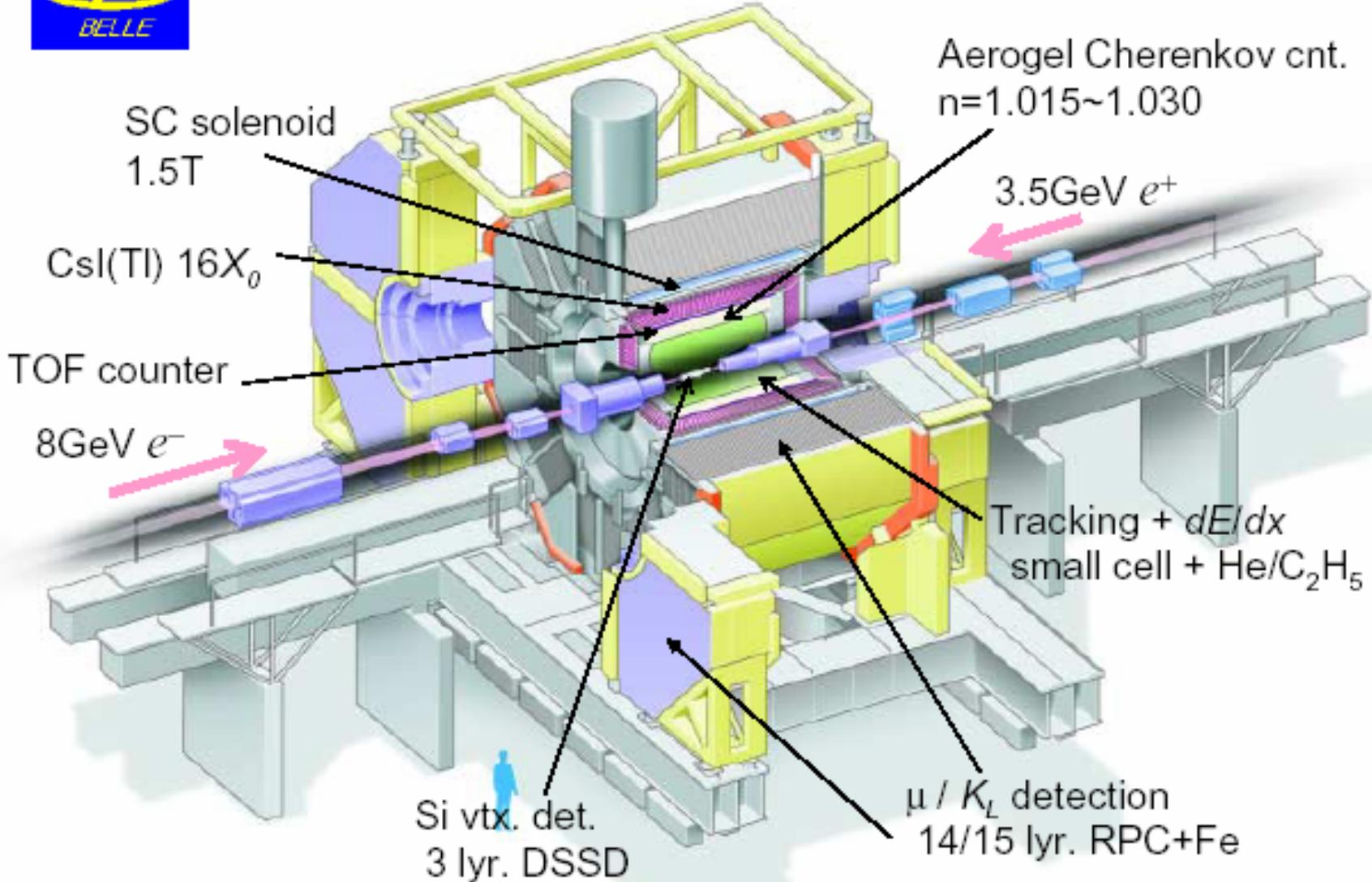
- Average Trigger rates:

$Y(4S) \rightarrow B\bar{B}$	11.5 Hz
$q \bar{q}$	28 Hz
$\mu\mu + \tau\tau$	16 Hz
<i>Bhabha</i>	4.4 Hz
2γ	35 Hz





Belle Detector



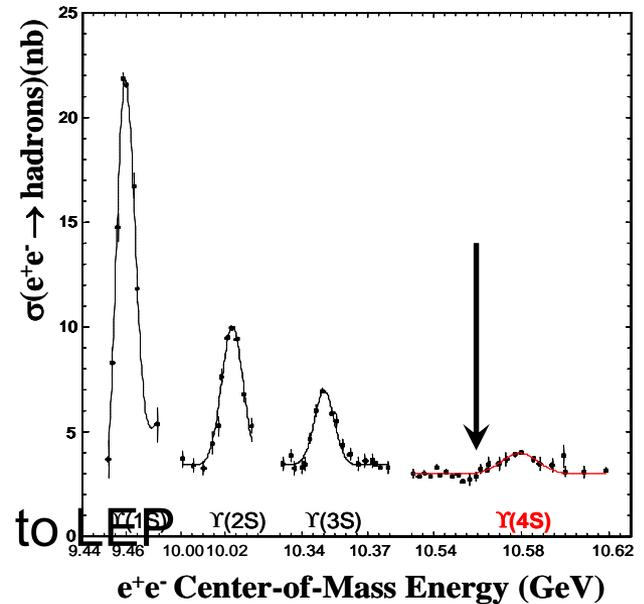
Good tracking and particle identification!





Belle is Well Suited for FF Measurements:

- Good detector performance (acceptance, momentum resolution, pid)
- Jet production from light quarks
→ off-resonance (60 MeV below resonance)
(~10% of all data)
- Intermediate Energy
→ Sufficiently high scale ($Q^2 \sim 110 \text{ GeV}^2$)
- can apply pQCD
→ Not too high energy ($Q^2 \ll M_Z^2$)
- avoids complication from Z interference
- Sensitivity = $A^2 \sqrt{N} \sim \times 25 \text{ (100)}$ compared to
 $A_{\text{Belle}} / A_{\text{LEP}} \sim \times 2$ (A scales as $\ln Q^2$)
 $\int L_{\text{Belle}} dt / \int L_{\text{LEP}} dt \sim \times 46 \text{ (600)}$



Total number of hadronic events $\sim 1.5 \times 10^9$



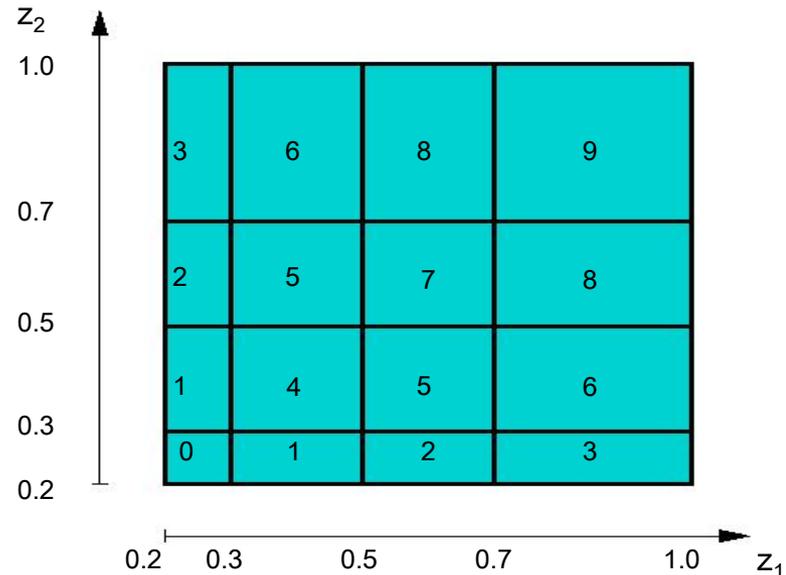
Applied Cuts, Binning

- Originally off_resonance data, now also on_resonance data (29.1 \rightarrow 547 fb⁻¹)
- Track selection:
 - pT > 0.1 GeV
 - vertex cut: dr < 2cm, |dz| < 4cm
- Acceptance cut
 - -0.6 < cosθ_i < 0.9
- Event selection:
 - Ntrack ≥ 3
 - Thrust > 0.8
 - Z₁, Z₂ > 0.2

- Hemisphere cut

$$(P_{h2} \cdot \hat{n}) \hat{n} \cdot (P_{h1} \cdot \hat{n}) \hat{n} < 0$$

- Q_T < 3.5 GeV
- Pion PID selection





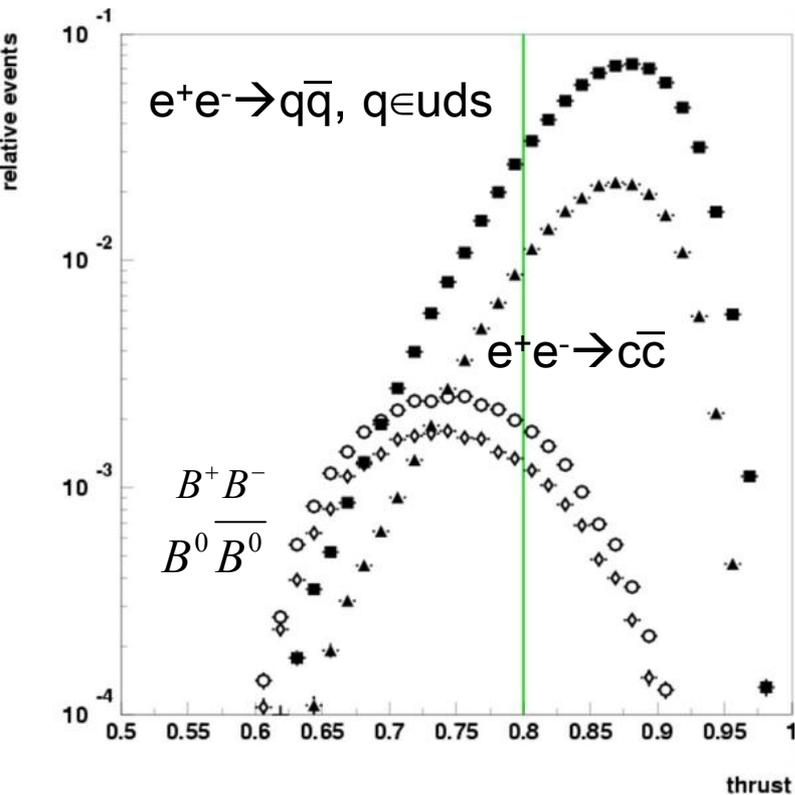
Experimental Issues

- $\cos 2\phi$ moments have two contributions:
 - Collins → Can be isolated either by subtraction or double ratio method
 - Radiative effects → Cancels exactly in subtraction method, and in LO of double ratios
- Beam Polarization zero? → $\cos(2\phi)$ asymmetries for jets or $\gamma\gamma$
- False asymmetries from weak decays → Study effect in τ decays, constrain through D tagging
- False asymmetries from misidentified hemispheres → Q_T or polar angle cut
- False asymmetries from acceptance → Cancels in double ratios, can be estimated in charge ratios, fiducial cuts
- Decaying particles → lower z cut

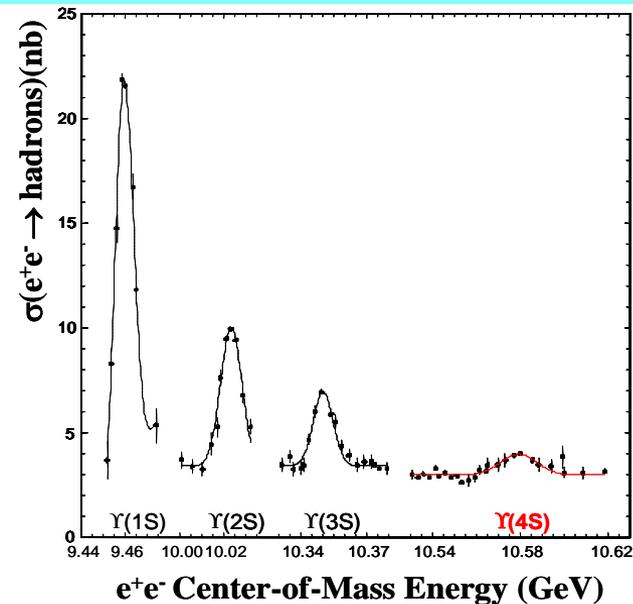




Why is it Possible to Include Data on Resonance? Different Thrust Distributions



$$\text{thrust} = \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$$



- small B contribution (<1%) in high thrust sample
- >75% of X-section continuum under Y (4S) resonance
- $29 \text{ fb}^{-1} \rightarrow 547 \text{ fb}^{-1}$
- many systematic errors reduce with more statistics
- Charm-tagged Data sample also increases

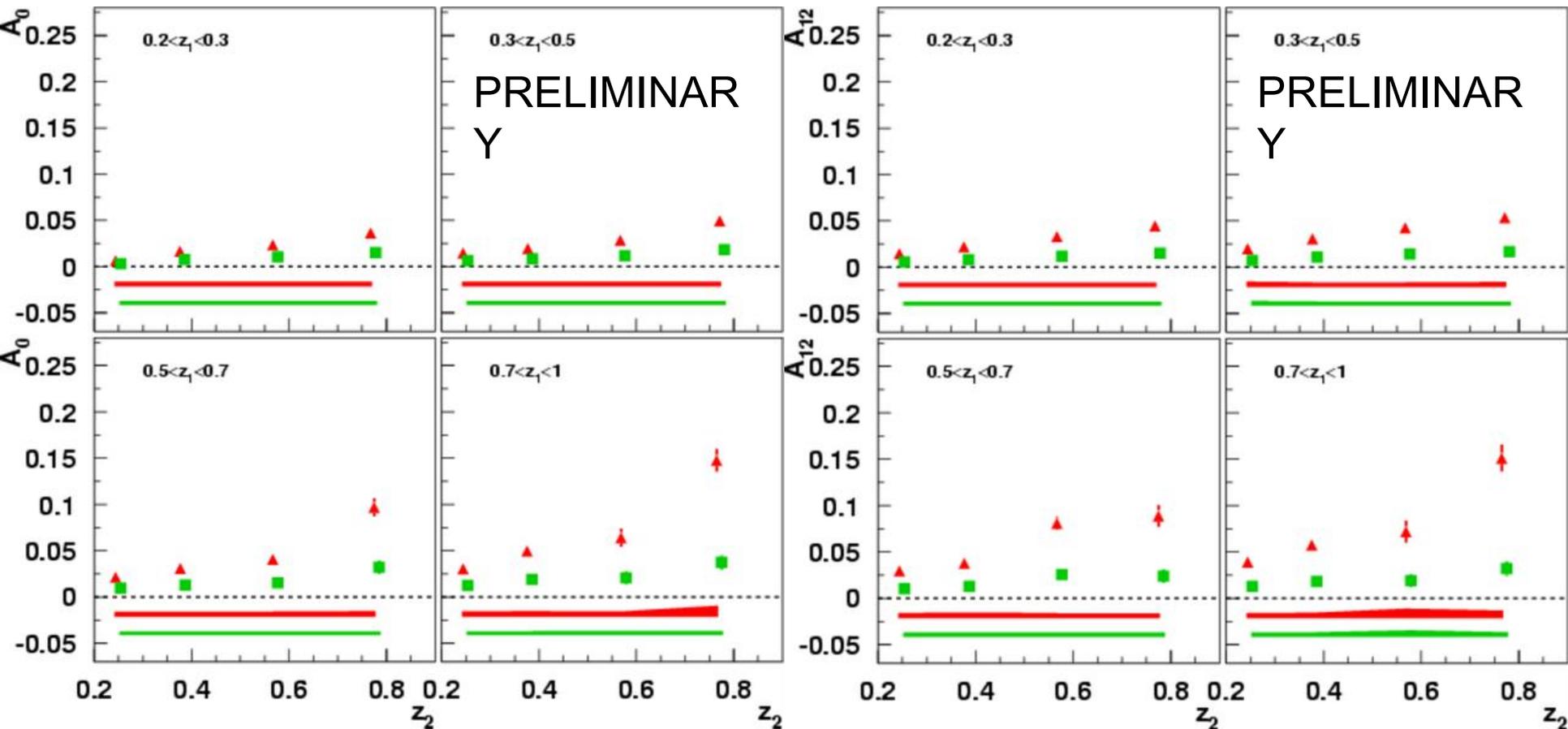




Collins Asymmetries I: 4x4 z_1, z_2 binning

$A_0(\cos(2\phi_0))$ moments

$A_{12}(\cos(\phi_1 + \phi_2))$ moments

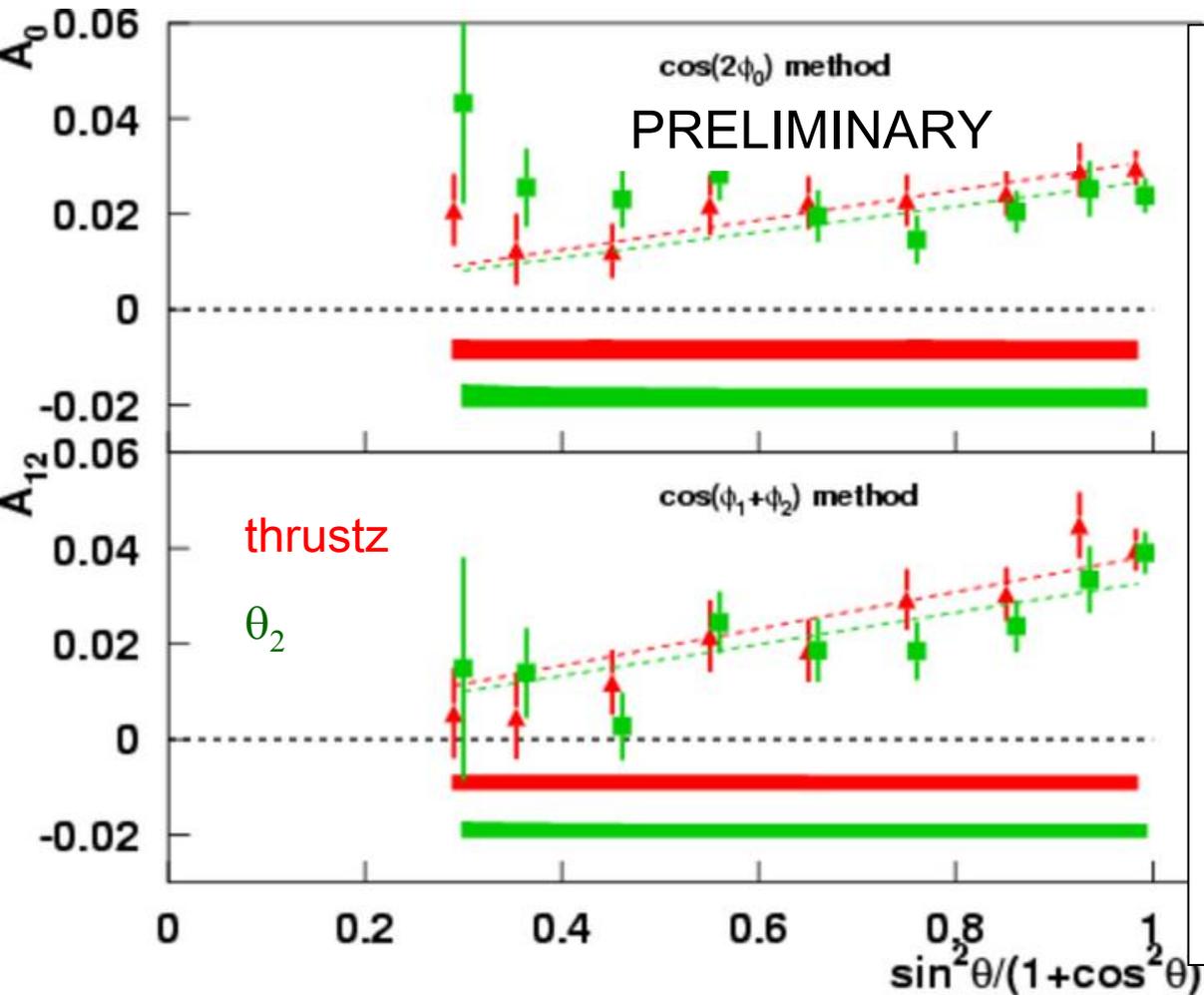


- 547 fb⁻¹ charm corrected data sample,
- UL and UC double ratios





Collins Asymmetries II: $\sin^2 \theta / (1 + \cos^2 \theta)$ Binning (UL)

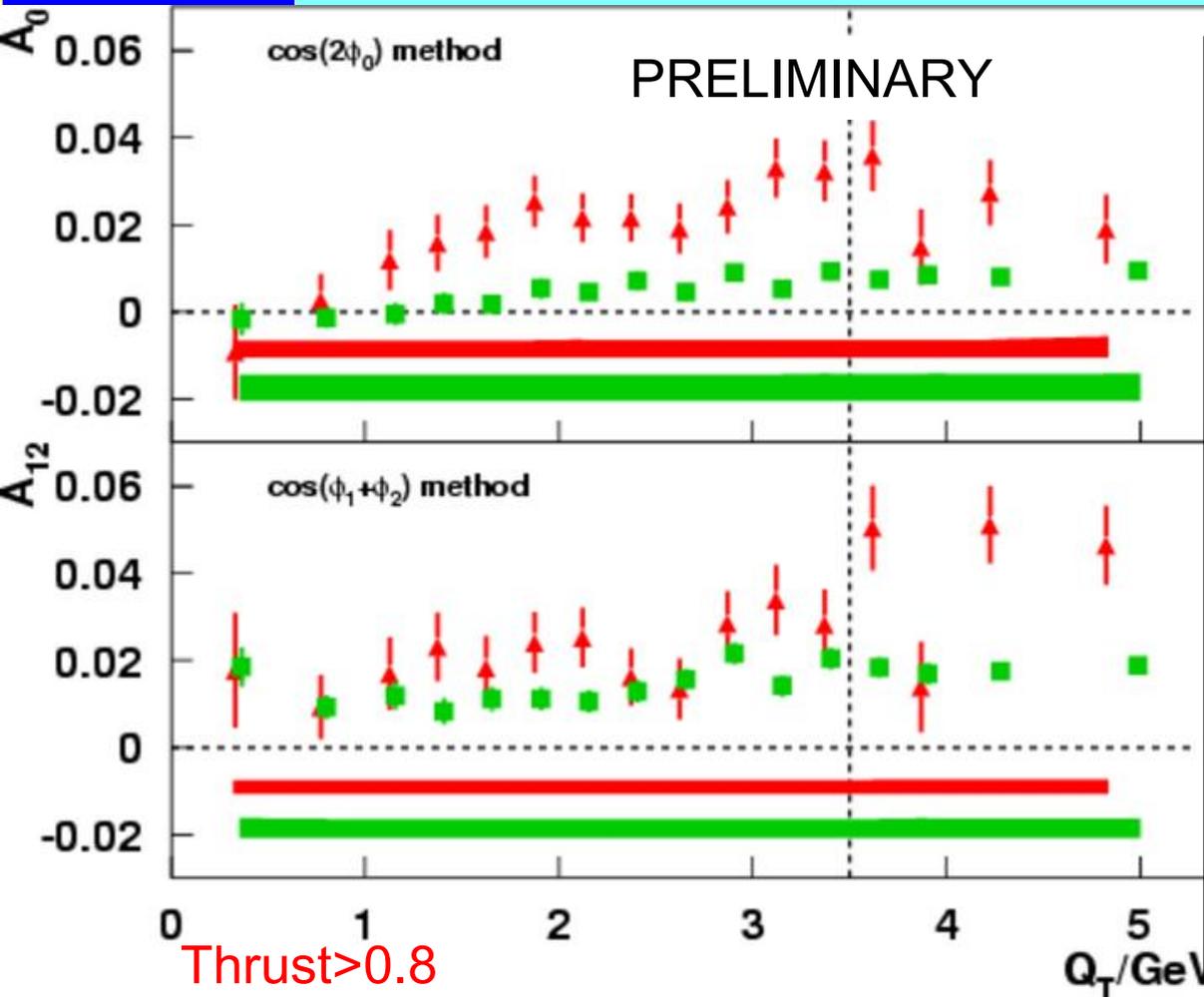


- Nonzero quark polarization $\sim \sin^2 \theta$
- Unpolarized denominator $\sim 1 + \cos^2 \theta$
- Clear linear behavior seen when using either **thrustz** or 2nd hadron as polar angle
- Better agreement for thrust axis (\sim approximate quark axis)
- UC plots similar





Collins Asymmetries III: Q_T Binning (UL)



- Reduced asymmetries in low thrust sample
- At low thrust significant B contribution
(for $t < 0.8$ ~20 % B
for $t > 0.8$ < 1 % B)
- A_{12} thrust axis dependent
- High Q_T (>3.5 GeV) asymmetries from beam related BG
- UC plots similar





Improved Systematic Errors (UC)

- Tau contributions
- PID systematics*
- MC double ratios
- Charged ratios ($\pi^+\pi^+ / \pi^-\pi^-$)
- Higher order terms
- Double ratio-subtraction method

Reweighting asymmetries:

→underestimation of $\cos(\phi_1+\phi_2)$
asymmetries →rescaled by 1.21

Correlation studies:

→statistical errors rescaled by 1.02 (UL)
and 0.55 (UC)

Beam polarization studies

→consistent with zero

